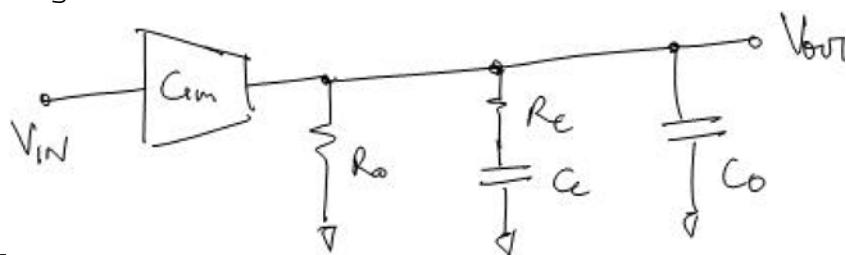


GM Amp loaded with Lead Lag network

Figure 1:



The equation is:

$$\begin{aligned}
 (%i1) \quad & e1: V_{out} = G_m V_{in} / (1/R_o + 1/(R_c + 1/(s*C_c)) + s*C_o); \\
 & \text{gain: rhs(ratsimp(e1/V_{in}))}; \\
 (%o1) \quad & V_{out} = \frac{G_m V_{in}}{C_o s + \frac{1}{\frac{1}{C_c s} + R_c} + \frac{1}{R_o}} \\
 (%o2) \quad & \frac{C_c G_m R_c R_o s + G_m R_o}{C_c C_o R_c R_o s^2 + ((C_o + C_c) R_o + C_c R_c) s + 1}
 \end{aligned}$$

Zero is:

$$\begin{aligned}
 (%i3) \quad & \text{zero: solve(num(gain), s)}; \\
 (%o3) \quad & [s = -\frac{1}{C_c R_c}]
 \end{aligned}$$

Poles are:

$$\begin{aligned}
 (%i4) \quad & \text{poles: solve(denom(gain), s)}; \\
 (%o4) \quad & [s = -\frac{\sqrt{(C_o^2 + 2 C_c C_o + C_c^2) R_o^2 + (2 C_c^2 - 2 C_c C_o) R_c R_o + C_c^2 R_c^2} + (C_o + C_c) R_o + C_c R_c}{2 C_c C_o R_c R_o} \\
 , s = & \frac{-\sqrt{(C_o^2 + 2 C_c C_o + C_c^2) R_o^2 + (2 C_c^2 - 2 C_c C_o) R_c R_o + C_c^2 R_c^2} + (-C_o - C_c) R_o - C_c R_c}{2 C_c C_o R_c R_o}
 \end{aligned}$$

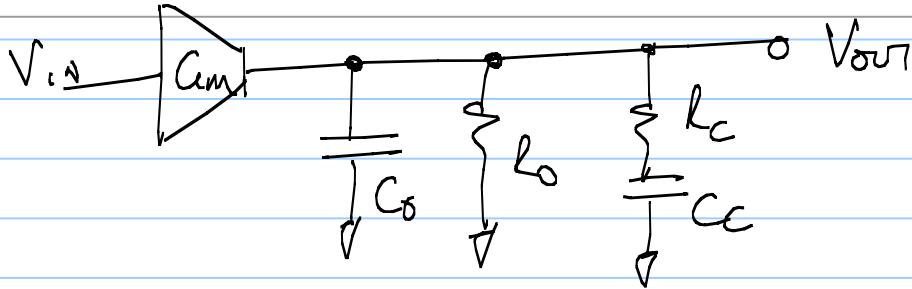
These can be approximated as: ($C_c \gg C_o$, $R_o \gg R_c$)

$$\begin{aligned}
 (%i5) \quad & \text{assume}(C_c > 0, R_c > 0, R_o > 0, C_o > 0); \\
 (%o5) \quad & [C_c > 0, R_c > 0, R_o > 0, C_o > 0]
 \end{aligned}$$

$$\begin{aligned}
 (%i6) \quad & \text{ratsimp(factor}([s = -(\sqrt{(C_c^2) * R_o^2 + (2 * C_c^2) * R_c * R_o + C_c^2 * R_c^2} + C_c) * R_o) \\
 (%o6) \quad & [s = -\frac{\sqrt{R_o^2 + 2 R_c R_o + R_c^2} + R_o}{2 C_o R_c R_o}, s = \frac{\sqrt{R_o^2 + 2 R_c R_o + R_c^2} - R_o}{2 C_o R_c R_o}]
 \end{aligned}$$

This can be further reduced as:

```
(%i7) ratsimp([s=-(Ro)+Ro)/(2*Co*Rc*Ro),s=(Ro)-Ro)/(2*Co*Rc*Ro)];  
(%o7) [s=-1/(Co Rc), s=0]
```



Poles:

$$\begin{aligned}s &= \pm \sqrt{(C_0 + C_c)^2 R_0^2 + 2C_c(C_0 - C_c)R_0 R_c + C_c^2 R_c^2} \\ &\quad \pm \frac{[(C_0 + C_c)R_0 + C_c R_c]}{2C_c R_0 R_c}\end{aligned}$$

$$s \approx \pm \frac{\sqrt{C_0^2 R_0^2 - 2C_0 C_c R_0 R_c}}{2C_c C_0 R_0} \pm C_0 R_0$$

$$s \approx \pm \frac{\chi_0 R_0 \left(\left(1 - \frac{2C_c R_c}{C_0 R_0} \right)^{1/2} \pm 1 \right)}{2C_c \chi_0 R_c R_0}$$

$$s \approx \pm \frac{1}{2C_c R_c} \left(1 - \frac{C_c R_c}{C_0 R_0} \pm 1 \right)$$

$$s \approx -\frac{1}{C_c R_c} \pm \frac{1}{2C_0 R_0}, \quad \frac{1}{2C_c R_c} \left(-\frac{C_c R_c}{C_0 R_0} \right)$$

$$s \approx -\frac{1}{C_c R_c}, \quad -\frac{1}{2C_0 R_0} \quad \text{Hence zero & pole are same!}$$